## Math Analysis I Honors- Midyear Review -

## Scientific Calculators Only! - Show all work!

1. Find the slope of the line $2 x-3 y+7=9$.
2. Find the slope of the line $5 y+12 x=4$.
3. Find the equation of the line parallel to $5 x+10 y=3$ with a $y$-intercept of 2 .
4. Find the equation of the line perpendicular to $5 x+10 y=3$ with a $y$-intercept of -1 .
5. Find the value of $A$ in the equation $3 x+A y=10$ if the point $(1,2)$ lies on the line.
6. Find the value of $A$ in the equation $y=2 A x^{2}+10$ if the point $(1,16)$ lies on the parabola.
7. Find the point of intersection between the lines $x-3 y=9$ and $2 x+2 y=-6$.
8. Find the point of intersection between the line $y=2 x+5$ and the parabola $y=8-x^{2}$.
9. Find the vertex of the parabola $y=2 x^{2}+4 x-10$.
10. Find the vertex of the parabola $y=x^{2}-10 x+1$.
11. Find the equation of the line through the points $(1,3)$ and $(-1,7)$.
12. Find the equation of the line through the points $(2,-3)$ and $(4,3)$.
13. The imaginary number $i^{20}$ is equal to:
14. The imaginary number $i^{33}$ is equal to:
15. Simplify $\sqrt{-32}$
16. Simplify $\sqrt{-50}$
17. Find the product of the complex numbers $(2+3 i)$ and $(4-i)$.
18. Find the product of the complex numbers ( $5-2 i$ ) and $(-2+3 i)$.
19. Solve for $x$ : $x^{2}+3 x=10$.
20. Solve for $x: 2 x^{2}+4 x-12=0$.
21. Find the minimum value of the parabola $f(x)=x^{2}-4 x-8=0$.
22. Find the maximum value of the parabola $f(x)=-x^{2}+3 x-18$.
23. At what points does $f(x)=x^{2}-8 x+15$ intersect the $x$-axis?
24. At what points does $f(x)=x^{2}+4 x-12$ intersect the x -axis?
25. Sketch a graph of the equation $f(x)=x(x+2)(x-1)$.
26. Sketch a graph of the equation $f(x)=(x+1)^{2}(x-4)(x-2)$.
27. Find the remainder when $2 x^{3}+5 x^{2}+4 x+1$ is divided by $x-3$.
28. Find the remainder when $3 x^{4}-3 x^{3}+6 x+2$ is divided by $x+2$.
29. Find a cubic equation with roots of 0,2 and -3 .
30. Find a quartic equation with roots of 2 and 4 , and a double root at -1 .
31. Why must a function with an odd degree have at least one x-intercept?
32. What is true about all irrational and imaginary (complex) roots?
33. How many x-intercepts can a quartic equation have?
34. What does a point where a polynomial's graph is tangent to the $x$-axis represent?
35. If $f(x)=3 x^{2}+k x-5$ and $f(3)=8$, what is the value of k ?
36. If $f(x)=x^{3}+x^{2}+4 x-2 k$ and $f(2)=18$, what is the value of $k$ ?
37. Solve the inequality $4 x-16>-7$.
38. Solve the inequality $-2 x+5 \geq 12$.
39. Find the solution set to the inequality $|2 x+5|<6$.

40 . Find the solution set to the inequality $|x-4| \geq 10$.
41. Solve the following polynomial inequality: $(x-1)^{2}(x+2)>0$.
42. Solve the following polynomial inequality: $(x+2)(x-3)(x-5)<0$.
43. Graph the solution to $2 y-3 x>12$.
44. Graph the solution to $3 y+6 x<10$.
45. Find the domain and range of the function $f(x)=|x|-3$.
46. Find the domain and range of the function $f(x)= \pm \sqrt{x+10}$.
47. If $f(x)=4 x-5$, find $f^{-1}$.
48. If $f(x)=x^{3}+4$, find $f^{-1}$.

For \#49-56, use $f(x)=x^{2}-3 x$ and $g(x)=4 x-5$.
49. Find $h(3)$ if $h(x)=[f(x)][g(x)]$.
50. Find $h(x)=(f+g)(x)$.
51. Find $f(g(3))$.
52. Find $g(f(-1))$.
53. Find $(f \circ g)(x)$.
54. Find $(g \circ f)(x)$.
55. Using $f(x)$ above, sketch the graph of $f(-x)$.
56. Using $f(x)$ above, sketch the graph of $|f(x)|$.
57. How does the graph of $\mathrm{y}=|x-2|-1$ compare to the graph of $y=|x|$ ?
58. How does the graph of $\mathrm{y}=x^{2}+3$ compare to the graph of $y=x^{2}$ ?
59. Graph the piecewise function $f(x)=\left\{\begin{array}{cc}x^{2} & \text { if } x \leq-2 \\ x-3 & \text { if } x>-2\end{array}\right\}$. Find $f(2)$ and $f(-5)$
60. Graph the following piece-wise function by hand. Then identify its domain, range, and zeros.

$$
f(x)=\binom{-x+2, \quad 1 \leq x<4}{x^{2}, \quad-2 \leq x<1}
$$

61. What is the domain of $\frac{3}{x+4}$ ?
62. What is the domain of $x^{2}+3 x-4$ ?
63. Solve for $x$ : $\quad 50=2(x-5)^{2}$
64. Simplify $\frac{6}{3+i}$
65. Write an inequality for the following graph $\rightarrow$
66. What types of functions have inverse functions?
67. If $\mathrm{f}(\mathrm{x})=2 \llbracket x \rrbracket-3$, find $\mathrm{f}(1 / 2), \mathrm{f}(\pi)$, and $\mathrm{f}(-3.2)$

68. How is the amplitude and fundamental period of a function found?
69. Simplify. Eliminate negative exponents.
a) $\left(-3 x^{3}\right)^{2} \cdot 3 x^{-8}$
b) $x z^{-3}\left(x z^{3}-4 z^{4}\right)$
c) $\frac{6 x^{1 / 2} y^{-1 / 2}-4 x^{2} y^{1 / 2}}{8 x y^{-3 / 2}}$
70. Change to exponential form and solve:
a) $\log _{2} 64=x$
b) $\log _{x} 32=5$
c) $\log _{81} x=1 / 2$
d) $\ln \mathrm{e}^{3}=x$
e) $\log 1000=x$
